### **Tension Analysis of Submarine Cables During Laying Operations**

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**Abstract:** This paper presents a semi-analytical approximation for a two-dimensional (2D) tension analysis of submarine cables during laying operations. In the analysis, based on geometric compatibility relations and equilibrium equations, a set of non-linear differential equations are obtained. The present model considers effects of ocean currents, cable ship motion, pay-out rate, water depth and material properties on submarine cable behavior in water, which are crucial during laying operations. As shown in numerical examples, with consideration of currents and cable ship motion, the cable tension appears to be smaller and cable configuration curve tends to be fatter than the conventional catenary theory.

Keywords: Submarine cable, Cable tension, Cable configuration.

#### 1. INTRODUCTION

In the last few decades, rapidly increasing expansions of telecom systems and exploitation of the oceanic natural resources demand intensive use of cables in marine environments. However, how to ensure the operation quality of submarine cable during laying operation is still a challenge issue in ocean engineering. With the significant commercial benefits, the analysis of submarine cable tension and profile during laying operations in water is very important. Once the analysis is available, it can effectively avoid some detrimental effects on submarine cables that will guarantee work quality as well as improve operation efficiency. Therefore, the tension analysis of submarine cables has been a great interest to civil engineering research for the past few decades.

Based on different assumptions, numerous theories have been developed for the static and dynamic response of submarine cable. Among these, Zajac [1] first developed a steady-state theory, in which the cable was modeled as a straight line and excluded the effect of transient motions. Following Zajac [1], many investigators have been trying different approaches to analyze both static and dynamic behaviors of submarine cables during laying operations. Among these, Yoshizawa and Yabuta [2] presented an analytical method for tension analysis of cables without considering the tangential drag forces, and the model was used to calculate the bottom tension due to negative slack. Their model showed that the bottom tension mainly depended upon the cable ship velocity and water depth, and the theoretical results were in good agreement with experimental results. Wang *et al.* [3] presented linear and nonlinear methods separately to build up a dynamic model. Based on forces and moment balance of the cable as a whole, governing equations were obtained. The relations of tension's effects on ship speed, cable's velocity and water depth were analyzed. Because the technical issues such as the speed and accuracy of cable laid are significant to commercial benefits, the analysis of transient behavior of cables becomes more important.

Vaz and Patel [4] developed a model for the prediction of the transient behavior of cables when the cable ship changes speed during towing operations. For the 2D model, it incorporates self-weight, normal and tangential drag forces, axial tension, geometric stiffness and physical added inertia when analyzing transient cable configuration and tension. Patel and Vaz [5] further developed a general 2D formulation in [4] for towed cables, and focused on the two-dimension model of cable laid, which is an extension of the former. Following the previous work for 2D model, Vaz et al. [6] presented a formulation and numerical solution for the 3D transient behavior of cable during laying operations when the cable ship changes speed and direction in calm water with the presence of currents, which adopted conventional finite element method and Runge-Kutta technique to solve the problem. Extending from [6], Vaz and Patel [7] developed the formulation and solution of governing equations used to analyze the 3D behavior of cables which are subjected to arbitrary sheared currents. Similarly, Wang et al. [8] presented an efficient numerical schemes-boundary condition transformed into a set of nonlinear governing equations with initial values.

The vertical movement of a cable ship caused by waveinduced vessel motion adds a non-ignorable tension force at the laying wheel. Prpic and his co-workers [9, 10] presented a two-dimensional model of cable dynamic accounting for the effects of head sea conditions. In their analysis, the verti-

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cal motion of the laying wheel point is of main importance, while the contribution of both longitudinal and transverse is neglected. However, the cable encounters the greatest tension during laying and recovering operations, Nagatomi et al. [11] presented a lumped mass method to analyze the motion and tension of the submarine cables, and compared with results of field experiment. Later, Yu and Tan [12] introduced a finite element model to analyze mooring cable dynamics and seabed interaction in time domain. The mooring cables are simulated by hybrid beam elements, while the seabed is simulated by different soil constitutive models. Chucheepsakul et al. [13] presented a variational model to analyze the three-dimensional steady state behavior of an extensible marine cable. Meanwhile, the finite element method and the shooting-optimization technique are employed to solve and evaluate the problem.

Park et al. [14] developed a 3D finite difference model and experimental investigation to solve the analysis of cable tension, considering the bending stiffness. Similarly, assuming the cable is not perfectly flexible; Dreyer and van Vuuren [15] accounted for the bending stiffness of the cable and adopted the rod model to calculate cable tension and configuration in water. As an improvement to the above work, Sun and Leonard [16] presented a general set of threedimensional dynamic field equations of submarine cables with flexural, torsional and inertia effects included. Croll [17] proposed an incremental boundary layer formulation to describe the nonlinear behavior of tensioned cables, rods and pipelines. In the analysis, boundary layers can be simplified to the bending of the tensioned cables. Based on elastic catenary theory, Bruno et al. [18] developed a full nonlinear model to analyze the nonlinear static behaviour of cable systems. Their model can be applied to many practical engineering fields, if the static equilibrium configuration of cable systems under environmental loads is given. Hao et al. [19] adopted the extrapolation method to analyze the effects of bending stiffness of the cable and current drag forces on cable tension and configuration, which required iterative computation until the accuracy satisfied permissible error. Similarly, Vairo [20] proposed a refined second-order model to obtain the elastic response of cables. Unlike the model mentioned in [19], the procedures had no need to iterative computation with taking into nonlinear cable-structure interaction effects. Based on classical secant model, Vairo [21] developed a non-linear continuous model for the analysis of long-span cable-stayed bridges. In the analysis procedure, both flexural and torsional terms had been taken into consideration. Zhang and Hu [22] proposed that the submarine cable operation can be performed through the tension control. Leonard et al. [23] presented a combined iterative and direct integration method to solve governing differential equations. With uniformly distributed loading, O'Brian [24] presented three different models, parabolic, elastic catenary and associate catenary. Most mentioned models just considered small deformation of cables, While Bouaanani et al. [25] presented a new approach which included large sag and extensibility effects and adopted the finite difference method.

In summary, most aforementioned models had some restrictions on engineering application. For example, linear model completely ignored the tangential drag forces, and assumed the elevation angle is constant along cable, which does not exist at all. The lumped mass method and finite element models adopted extrapolation method to iterative computations, which must be completed under suitable assumptions. In other words, in the analysis process, some initial value should be constantly adjusted to satisfy all the boundary conditions.

In this paper, a semi-analytical approximation is proposed for the prediction of tension and cable configuration during laying operations. With a set of differential equations obtained, a non-linear model is built up to simulate the problem. With initial values, explicit iterative method is proposed to calculate the elevation angles of different cable segments, then, cable configuration and tension distribution in water can be obtained. A comprehensive comparison between the present and previous models is performed and shows good in agreement. A parametric study will be conducted to examine the effects of ocean current and wave characteristics on cable tension and profile.

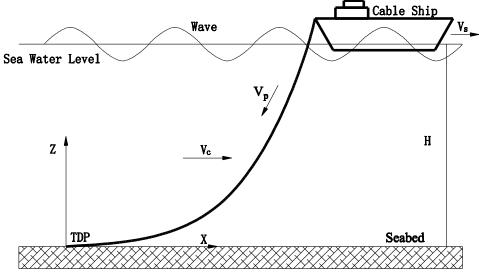


Fig. (1). Sketch of cable laying operations.

### 2. THEORETICAL MODEL

### 2.1. Problem Considered

The present theory can be used to solve some relevant problems about submarine cable in engineering application. Based on the calculations, tension distribution and cable configuration in water during laying operations can be obtained. The problem considered in this study is illustrated in Fig. (1). In the figure,  $V_c$  is current velocity,  $V_s$  is cable ship motion, H is water depth,  $V_p$  is payout-rate, and  $\omega$  is self-weight of the cable.

In this study, the tension analysis of submarine cable is based on the following assumptions:

- Continuous: submarine cable is considered continuous in the analysis;
- Inextensible: because of relatively high axial stiffness, cable extensible can be neglected in the analysis;
- Flexible: bending stiffness is neglectful;
- Cable and body dimensions are small compared to incident wave length, so calculation of hydrodynamic forces by the Morison equation is valid;
- The seawater is ideal liquid: irrational, inviscid and incompressible;
- Submarine cable: rotational motions are not considered, cable weight per unit length is constant and cross-sectional area is uniform;
- The submarine cable is taken to be fully immersed in water, no portion of cable above the seawater level is

taken into consideration in this analysis;

- Submarine cable is subjected to uni-axial tension without flexure, shear or torsion;
- Drag forces on the cable are taken from the relative velocity form of the Morison equation, and the independence principle for normal and tangential drags is invoked;
- The drag coefficients Cn and Ct in the Morison equation are Reynolds number dependent, but in this paper, they are taken as constant values;

# 2.2. Equilibrium Equations for the Submarine Cable in Water

When the submarine cables are laid from the laying wheel point on a cable ship, there are at least four components that contribute to the tensional forces along the submarine cable.

- Gravity forces, which is due to submarine cable self-weight;
- Buoyancy force, which is equal to the weight of its displaced fluid;
- Drag forces, which are due to steady current and current profile;
- Residual bottom tension, which translates to an extra tensional force during the laying operations;

Considering a cable infinitesimal element, its equilibrium state is shown as in Fig. (2); in the tangential (t) and mal (p) directions, respectively.

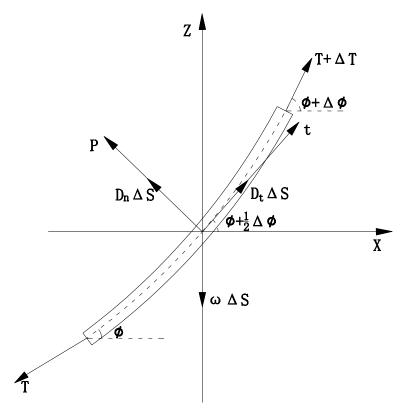


Fig. (2). Forces acting on the submarine cable in seawater.

$$(T + \Delta T)\cos\frac{\Delta\varphi}{2} + D_t \cdot \Delta S - \omega\Delta S \cdot \sin\left(\varphi + \frac{\Delta\varphi}{2}\right) - T\cos\frac{\Delta\varphi}{2} = 0$$
(1)
$$(T + \Delta T)\sin\frac{\Delta\varphi}{2} + D_t \cdot \Delta S - \omega\Delta S \cdot \cos\left(\varphi + \frac{\Delta\varphi}{2}\right) + T\cos\frac{\Delta\varphi}{2} = 0$$
(2)

where T is the tension force at a i-th point;  $\omega$  is self-weight of submarine cable per unit length in water;  $\Delta T$  and  $\Delta \varphi$  are the difference tension and elevation angle between i-th and i+1-th points;  $\Delta S$  is the arc length of cable element; and  $D_t$  and Dn are drag forces in tangential and normal directions, respectively.

When the element length tends to be infinitely small (i.e., approaching to a point),  $\Delta \phi \rightarrow 0$ , then  $\sin \Delta \phi \approx \Delta \phi$ , and  $\cos \Delta \phi \approx 1$ , then (1) and (2) can be simplified as

$$\frac{\partial T}{\partial S} = (\omega \cdot \sin \varphi - D_t), \frac{\partial \varphi}{\partial S} = \frac{1}{T} (\omega \cdot \cos \varphi - D_n)$$
(3)

Then tangential and normal drag forces per unit length in seawater can be acquired through Morison equation

$$D_t = \frac{1}{2} C_t \rho_\omega \pi D \cdot V_t^2, D_n = \frac{1}{2} C_n \rho_\omega D \cdot V_n^2$$
<sup>(4)</sup>

where Ct and Cn are drag coefficients in tangential and normal directions, which mainly depend on the Reynolds number and the roughness of submarine cable surface.  $\rho_{\omega}$  is density of seawater, D is effective diameter of submarine cable; Vn and Vt are relative velocity components in normal and tangential direction, respectively. In this paper, we adopt Cn = 1.50 andCt = 0.03, respectively [21].

In the Morison equation, the relative velocity is taken into consideration,

where

$$V_t = V_p - V_{cs} \cos \varphi, V_n = V_{cs} \sin \varphi$$
(5)

where V<sub>cs</sub> is the relative velocity between ocean current and cable ship motion in the sailing direction.

Since the tangential force is relative small, in the first step of tension calculation, the tangential force can be neglected, or Dt = 0. Then, (3) can be reduced to

$$\Delta T^* = \omega \cdot \sin \varphi^* \Delta S, \, \Delta \varphi^* = \frac{1}{T^*} (\omega \cos \varphi^* - D_n) \Delta S \tag{6}$$

where T<sup>\*</sup> is the submarine cable tension at an arbitrary point corresponding to elevation angle  $\varphi^*$  with Dt = 0.

Based on (6), we can obtain the following expression:

$$\frac{1}{T^*}dT^* = \frac{\omega\sin\varphi^*}{\omega\cos\varphi^* - D_n}d\varphi^* \tag{7}$$

The result of (7) is integrated over the cable element:

$$\int_{T_0}^{T} \frac{1}{T^*} dT^* = \int_{\varphi_0}^{\varphi^*} \frac{\omega \sin \varphi^*}{\omega \cos \varphi^* - D_n} d\varphi^*$$
(8)

And then tension of submarine cable can be expressed as:

$$T^* = T_0 \left[ \frac{2k_d \cos \varphi^* + \omega - m}{2k_d \cos \varphi^* + \omega + m} \cdot \frac{2k_d \cos \varphi_0 + \omega - m}{2k_d \cos \varphi_0 + \omega + m} \right]^{-\frac{\omega}{m}}$$
(9)

Where 
$$k_d = 0.5\rho_{\omega}C_n DV_{cs}^2$$
 and  $m = \sqrt{\omega^2 + 4k_d^2}$ .

where T0 and  $\varphi_0$  are the tension and elevation angle at the touchdown point (TDP), respectively. The relationship between submarine cable tension and water depth can be obtained through the following equilibrium equation:

$$T^* = T_0 + \omega \cdot H \tag{10}$$

Based on (7) and (8), the relation between cable elevation angle and water depth can be expressed as

$$\cos\varphi^* = \frac{m/k_d}{1 - \frac{2k_d\cos\varphi_0 + \omega - m}{2k_d\cos\varphi_0 + \omega + m}(1 + \omega h/T_0) - m/\omega} - \frac{\omega + m}{2k_d}$$
(11)

It is noted that the elevation angle determined from (9) doesn't consider the tangential force, i.e., Dt = 0. Therefore, we can further estimate the elevation angle for the case of  $D_t \neq 0$  by  $\varphi_i = \frac{1}{2}(\varphi_{i-1}^* + \varphi_i^*)$ .

Once the elevation angle  $(\varphi_i)$  at arbitrary point (with Dt) is obtained, the cable tension distribution can be determined based on (3),

$$T = T_0 \cdot e^{\int_{\phi_0}^{\phi} \frac{\omega \sin \varphi - K_t \cdot (V_p - V_{cS} \cos \varphi)^2}{\omega \cos \varphi - k_d \cdot V_{cS}^2 \sin^2 \varphi} d\varphi}$$
(12)

## **2.3.** Tension Calculation of a Submarine Cable During Laying Operations

As derived in the previous section, the cable tension can be determined by (12). Since an integration appears in the equation, it is impossible to obtain a close-form analytical solution. Therefore, in the present model, the submarine cable is discretized into N segments with the same dZ = H/N, where H is water depth. As shown in Fig. (3), the end point of each segment is numbered by index "i", which ranges from 0 at the touchdown point to N at the laying wheel point. The coordinate of the TDP is set as (0, 0).

According to the vertical coordinate,  $Z_i$  at numbered i-th point, the difference iterative equations are selected as follows. Provided that coordinate Z ranges from 0 to H, the iterative equations are:

$$\Gamma_{i+1} = \Gamma_i + T_0 \cdot e^{\int_{\varphi_i}^{\varphi_{i+1}} \frac{\omega \sin \varphi - K_t \cdot (v_p - v_{cs} \cos \varphi)^2}{\omega \cos \varphi - k_d \cdot v_{cs}^2 \sin^2 \varphi} d\varphi}$$
(13)

Then, (13) can be calculated through numerically by the Simpson method. In the calculation, the submarine cable is divided into N segments. Based on geometric compatibility, the coordinates of its segments along the cable are also determined.

$$Z_i = Z_{i-1} + \Delta Z_i, X_i = X_{i-1} + \Delta X_i, S_i = S_{i-1} + \Delta S_i$$
(14)  
where  $\Delta Z_i = H/N, \quad \Delta S_i = \Delta Z_i / \sin \varphi_i, \text{ and } \Delta X_i = \Delta Z_i \cot \varphi_i.$ 

To solve the above governing equations, appropriate boundary conditions are required for the analysis, and provided that the cable ship operates in uniform current. Firstly, at the touchdown point (TDP), the coordinate is assumed to be (0, 0), simultaneously  $T_0$  and  $\varphi_0$  should also be given. Secondly, at the laying wheel point, the value of vertical coordinate is given as H, or the seawater depth. Based on appropriate initial values, the problem can be effectively solved. In addition to boundary conditions, five initial conditions are required at the TDP, i.e. pre-tension ( $T_0$ ), elevation angle ( $\varphi_0$ ), water depth (H) and two Cartesian coordinates. The flow chart of cable tension calculation is shown in Fig. (**4**).

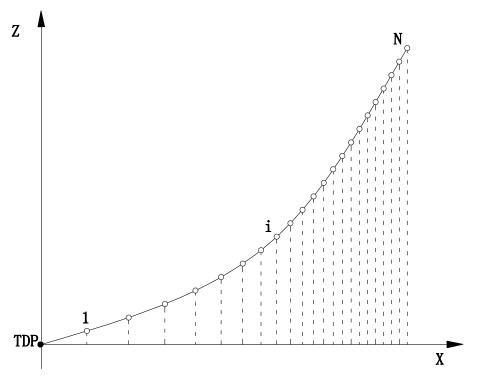


Fig. (3). Segment division of submarine cable during laying.

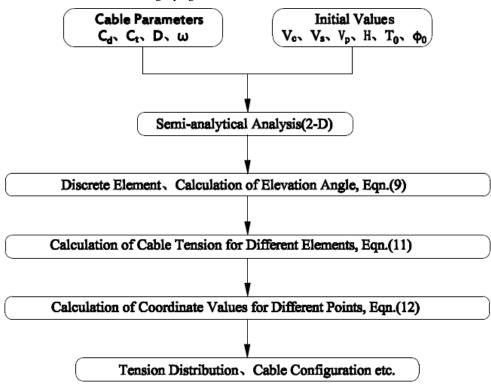


Fig. (4). Flow char of cable tension calculation.

#### 3. RESULTS AND DISCUSSIONS

#### 3.1. Comparison with Hao et al. [19]

Hao *et al.* [19] adopted an extrapolation method to analyze the problem. With a given initial value of elevation angle at TDP, the extrapolation method was proposed to confirm whether the calculated vertical coordinate of the laying

wheel point equals water depth (H). If not, a new value of  $(\varphi_0)$  is given, the above process is continuously repeated until the vertical coordinate of laying wheel point approximates water depth. In Hao's model [19], the axial stiffness was neglected, although it may have significant effects on the prediction of cable tensions. The input data used in the comparison is tabulated in Table 1.

 Table 1.
 Input Data for Comparison

Parameter	Value
Effective Diameter (D)	38 mm
Water depth (H)	20.0 m
Cable weight in water $(\omega)$	76.45 N/m
Normal drag coefficient (Cn)	1.2
Tangential drag coefficient (Ct)	0.024
Pre-tension (T0)	15.4 kN
Relative velocity (Vcs)	1.2 m/s

Based on the input data given in Table 1, the origin of Cartesian coordinate is located at the touchdown point on seabed. Cable tension and Cartesian coordinates are calculated, and the results are shown in Fig. (5). In the figure, the solid line represents the present theory and the dash line is for Hao *et al.* [19]. Fig. (5a) shows that cable configuration obtained from both models are almost identical. It is found in Fig. (5b) that cable tension calculated from the present theory is larger than that from Hao *et al.* [19] except for a very small portion around the seabed surface. The difference becomes slightly larger as X increases. At the water surface point, tension forces are 16.77 kN from [18] and 16.93 kN from the present theory, respectively.

### **3.2. Effect of the Relative Velocity Between Currents and Cable Ship Motion (Vcs)**

The conventional method used in the tensional analysis of the cables in marine environment was based on catenary theory [26]. In the approach, the cable is following a catenary line from the exit point on the laying wheel down to the TDP on the seafloor, by assuming the cable laying vessel lays cable in calm waters with constant speed over a horizontal seafloor. The cable is assumed to have no bending stiffness and no drag while moving through the water. In the following examples, we will compare the present model with the conventional catenary theory through a parametric study. The input data are listed in Table **2** unless they are specified.

Table 2. Input Data for the Parametric Study

Parameter	Value
Effective Diameter (D)	98 mm or various
Water depth (H)	60.0 m
Cable weight in water $(\omega)$	209 N/m or various
Normal drag coefficient (Cn)	1.50
Tangential drag coefficient (Ct)	0.03
Pre-tension (T0)	8 kN or various
relative velocity (Vcs)	1.2 m/s or various
Cable pay-out rate (Vp)	0.8 m/s or various

To have a deeper insight into the submarine cable behavior during laying operation, the effect of relative motion is studied here. In this example, five cases (catenary theory,  $V_{cs} = 0.4$  m/s, 0.8 m/s, 1.2 m/s, 1.6 m/s) are considered. As shown in Fig. (6), the difference between the present theory and catenary theory [26] can be observed. By comparing the calculated results, it can be observed that cable configuration of catenary theory is steeper than any relative velocity. Within 4.5 m above the seabed surface, cable profiles almost overlap, and the difference becomes larger as the relative velocity decreases. Similarly, the trend can be seen from Fig. (6b & c). However, the effects of relative velocity on the cable configuration are more important than that on tension distribution.

#### **3.3.** Effect of Cable Self-weight (ω)

Cable weight per unit length in water is another key parameter in the analysis of cable behavior during laying operations. Three different cable weights ( $\omega$ =145.0 N/m, 215.0 N/m, 297.0 N/m) are considered in this example. The corresponding mass of unit length, weight of cables in air, and effective diameter of cable are given in Table **3**.

Example presented in Fig. (7) shows that the influence of cable weight per unit length in water on tension distribution along water depth between two models are insignificant. Compared with the tension distribution, the cable weight has a more significant influence on cable configuration. As

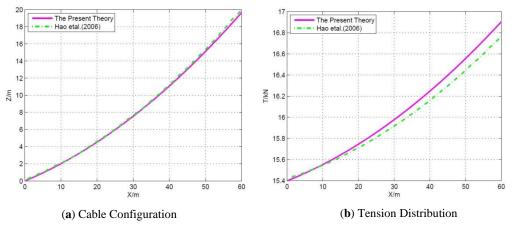


Fig. (5). Cable configuration and tension distribution from the present model and Hao et al [19].

shown in Fig. (7a), the difference between these two models can be observed. The difference becomes larger as X increases in cable configuration. It can be seen from Fig. (7a) that a heavier cable causes a steeper configuration curve. Similar trends can be found in the distribution of tension along the arc length, as shown in Fig. (7c).

#### 3.4. Effect of Pre-tension at TDP (T0)

During laying operations, the bottom tension at TDP can be measured by tensiometer. The bottom tension is considered as a critical parameter during laying. A lower bottom tension can cause the cable to build lops or snake, while a higher one will result in a highly residual tension in the ca-

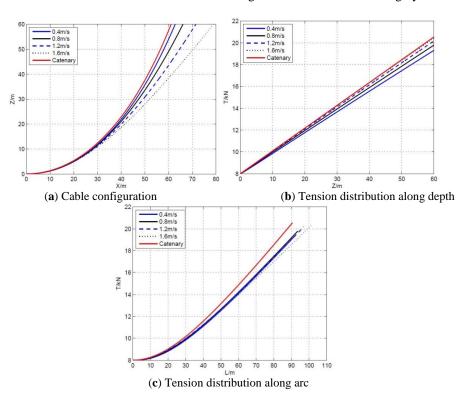


Fig. (6). Cable configuration and tension distribution with various relative velocities.

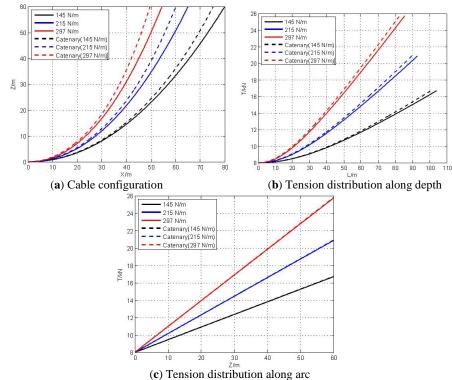


Fig. (7). Cable configuration and tension distribution with various self-weight.

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ble. Furthermore, the highly residual tension is thought to cause detrimental effects on cable during laying or in service, as well as impede burying for protection. To ensure operation quality, it would be best to adjust T0 to an optimum value.

In order to have a deeper insight into the contribution of the pre-tension at TDP to cable tension, four cases are illustrated in Fig. (8), i.e., T0 =6.0kN, 8.0 kN, 10.0 kN and 12.0 kN. As shown in Fig. (8b), tension almost increases linearly along water depth. Furthermore, for both catenary and the present theory, tension distributions are exactly consistent with each other when T0 equals 12.0 kN. While the relative difference value among different pre-tensions appears to be larger along X in configuration, while decreases with the increase of arc length in Fig. (8c).

#### 3.5. Effect of Cable Pay-out Rate (Vp)

The influence of cable pay-out rate on submarine cable is investigated and illustrated in Fig. (9). Different pay-out rates, 0.4 m/s, 0.8 m/s, 1.2 m/s, 1.6 m/s, are considered. With the decrease of pay-out rate, the tension distribution along water depth is approaching to the results under catenary theory. As for the cable profile, due to that the pay-out rate is tangent to cable configuration curve, as well as the tangential drag coefficient (Ct = 0.03) is relative too small, therefore, its contribution to cable configuration can be completely ignored. Furthermore, as shown in the figure, a faster pay-out rate will generate a smaller the tension force along cable, but no larger than those of catenary theory, in which situation the pay-out rate (Vp) is considered as zero. This implies that the conventional catenary theory is more conservative for operation.

#### Parameter Value Mass of unit length 40 kg/m 30 kg/m 20 kg/m Cable weight in water ( $\omega$ ) 296.7 N/m 215.2 N/m 145.5 N/m Cable weight in air 392.24 N/m 294.18 N/m 196.12 N/m Effective diameter of the cable (D) 110 mm 100 mm 80 mm 26 6.0kN 6 0kN 8.0kN 24 8.0kN 10 0kN 10.0kN 50 12.0kN ..... 12.0kN 22 Carenary(12.0kN) Carenary(12.0kN) 20 40 18 m/Z L/kN 30 20 10 20 30 40 50 60 70 80 90 10 20 30 40 50 60 (a) Cable configuration (b) Tension distribution along depth 6 OkN - · 8.0kN 24 10.0kN 12.0kN 22 Carenary(12.0kN) 20 18 **Γ/kN** 20 30 40 50 60 70 80 90 100 1/10

#### Table 3. Corresponding Properties of Cable Self-weight

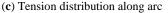


Fig. (8). Cable configuration and tension distribution with different pretension.

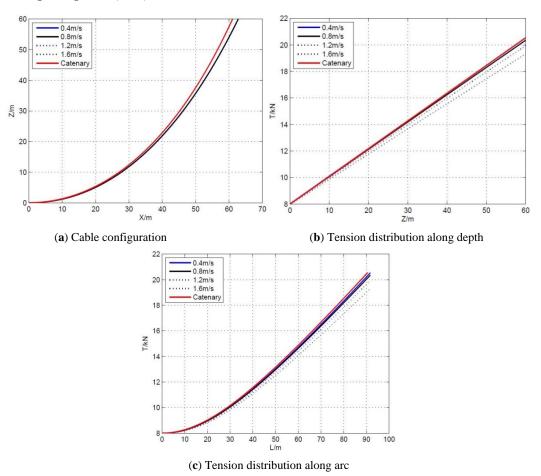


Fig. (9). Cable configuration and tension distribution with different pay-out rate (Vp).

#### CONCLUSIONS

In this study, a 2D semi-analytical approximation for submarine cable was developed for the prediction of the configuration and tension distribution during laying operations. In the present model, the comprehensive effects of ocean currents, water depth, cable ship motion, material properties were taken into consideration. Comparisons between the present model and the conventional catenary theory were presented through a parametric study.

Based on numerical examples presented, we found that : (1) The cable's tension almost varies linearly with the water depth, and reaches the maximum value at the laying wheel point; (2) Because of the tangential drag force being relative small, cable pay-out rate barely affects the cable configuration in water, while it is somewhat sensitive to the values of cable tension force; (3) Pre-tension at TDP has notable effect on cable's tension force and cable configuration, and the effect will be weakened with the increase of distance apart from the touch-down point; (4) At certain water depth, the relative velocity between current and cable ship is of great importance to the security of operation at sea; the faster the velocity, the larger the cable's tension, which will result in serious damage to marine cable; while the slower the velocity, the more costly the cable laying operation, which should be weighted by the operators carefully.

The present thesis studied 2D steady state motion under a variety of external forces. However, for elastic and flexible marine cables, mechanical response can be strongly changed and deeply affected when a significant variation of environment temperature occurs, which can be referred to Vairo *et al.* [27] and Bouaanani *et al.*[28]. Generally, the effects of thermal loads on cables can be classified into two ways: on one hand, the variation in temperature along the cable axes can lead to extensible deformation in cables. On the other hand, the difference in temperature on cable's surface will bring to bending deformation. Both effects can bring about a lack of effectiveness and accuracy in cable's tension analysis. For the future work, we will focus on developing a more effective numerical scheme to analyze the thermal effects on marine cable.

#### **CONFLICT OF INTEREST**

The authors confirm that this article content has no conflicts of interest.

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