

Analytic Hierarchy Process Application for the Selection of a Metal Matrix Composite

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Abstract: The multi-attribute decision-making methods allow to solve arbitrary problems governed by several parameters. In this paper, the choice of a composite material was analyzed, by considering the availability from four companies. The multi-attribute decision Analytic Hierarchy Process (AHP) procedure was used to select the best levels for different attributes, both parametric and non-parametric, and to select the best company.

Keywords: Analytic Hierarchy Process (AHP), decision-making methods, metal matrix composites.

INTRODUCTION

The production of composite materials falls within the “special processes” [1-3] category, which is important for the continuous monitoring of the process parameters. In practice, it is not possible to separate the calculation and optimization of the product from the production phase, as the parameters that affect the latter demand preliminary analysis and optimization during the design process. The optimization of the design and the production of mechanical components made of composite materials requires therefore to search for new methods of analysis, which allow to address the choice of the parameters and provide an effective procedure that enables the assignment of an index of the product quality. These methods must take into account the relative importance and the interactions between the various design and construction parameters, such as cost, purchased material characteristics, availability of processing factors. Moreover, since many parameters affect the processes of design and construction of the mechanical components made of composite materials, it is mandatory to take care in first place of the quality analysis of the supply, the availability of materials and the costs. To this field belongs the research, the adoption and the optimization of methods for the material selection, to assess and weigh the various factors affecting the purchase phase of the material. The methodology for Multi-Attribute Decision Making (MADM) is divided into elementary multi-criteria methodologies (score and lexicographic method) such as Multiple Attribute Utility Theory (MAUT) method, Analytic Hierarchy Process (AHP), Fuzzy Multi-Attribute Decision Making (FMADM), and “outranking” interactive methods. In particular, the Analytic Hierarchy Process (AHP) methodology [3-13] has been found to be the most suitable for the evaluation of the supplies of different companies producing materials and

metal matrix composites reinforced by alumina hard particles in different percentages [14-16].

The aim of this paper is to provide the designer with a practical tool that allows the selection of a particulate metal matrix composite material by considering the mechanical parameters, costs and availability offered by different dealers. This paper reports the application of a general procedure that any machine designer could use, without targeting at a specific application. Many other parameters, such as “corrosion resistance” and “ease of machinability”, might to be added, targeting at specific applications.

FUNDAMENTAL PARAMETERS (QUALITY INDEXES) FOR THE MATERIAL SELECTION

The most relevant parameters for the material selection have been divided into three different categories: mechanical characteristics, costs, availability.

The density of the material is used in the definition of the parameters related to the mechanical characteristics, since this factor seems to be important for the choice of the material itself. The considered factors are listed below:

- Mechanical Properties
 - 1) Modulus of longitudinal elasticity E , obtainable from tensile tests. This feature is very important, since the particle reinforced composite is chosen primarily for the high stiffness increase it offers. The ratio $\frac{E}{\rho}$ (where E is the modulus of longitudinal elasticity expressed in MPa and ρ is the material density in kg/m^3) is defined. The ratio is then normalized by imposing an optimal value of E (reference) equal to 10^5 MPa, as well as the density of the material, constant and equal to 2900 kg/m^3 .
 - 2) Percentage elongation at break $A\%$. An optimum value (reference) of elongation percentage equal to 10% is imposed, therefore the quality index takes the value 1 when $A = 10\%$.

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- 3) $\frac{R_m}{\rho}$ ratio, where R_m is the ultimate tensile strength in

MPa, obtainable from tensile tests, and ρ is the material density in kg/m^3 . The ratio is normalized by requiring that the density is constant and equal to 2900 kg/m^3 for the test material (otherwise, if this parameter is variable, a reference density can be defined) and that the optimal value of the breaking load is equal to 400 MPa.

- 4) $\frac{R_s}{\rho}$ ratio, where R_s is the yield strength in MPa

obtainable from tensile test and ρ is the material density equal to 2900 kg/m^3 . A reference value for the material yield strength, equal to 350 MPa, and a constant density, equal to 2900 kg/m^3 , are imposed, coherently with step 3.

- 5) $\frac{\sigma_{FA}}{\rho}$ ratio, where σ_{FA} is the fatigue strength of the

material for alternating load, in MPa, as measured by rotating bending fatigue tests with hourglass specimens, following the ISO 1143 requirements, and ρ is the density of the material in kg/m^3 . Since this index is defined as in step 3, a reference value of the fatigue limit of the material equal to 200 MPa, and a constant density equal to 2900 kg/m^3 are imposed.

- 6) Material uniformity, defined as a measure of a more or less homogeneous dispersion of the particles within the matrix, estimated by analyzing flat sections cut from some samples of the material. In order to estimate the homogeneity of the material, plane sections of area of 0.01 mm^2 (for example, a square cross section of side 0.1 mm) are examined by means of optical microscopy. The sections can be obtained from the extruded bars of W6A20A. From these sections, the total number of clusters of particles of size greater than $100 \mu\text{m}$ (the reinforcing particles have an average size of $20 \mu\text{m}$), as well as the number of clusters of particles with maximum size exceeding $100 \mu\text{m}$ for each section, can be determined. From the analysis, the values of $N_{100\mu\text{m}}$, *i.e.* the total number of clusters larger than $100 \mu\text{m}$, and of $N_{100\mu\text{mmax}}$, *i.e.* the maximum number of clusters larger than $100 \mu\text{m}$ found in a section, are derived. The following indexes can be defined:

- a) $\frac{N_{100\mu\text{m}}}{n}$, by imposing $n = 10$ and a reference value of $N_{100\mu\text{m}}$ equal to 1, the index takes the value 1 when the ratio is equal to 0.1.

- b) $\frac{N_{100\mu\text{mmax}}}{n}$, by imposing $n = 10$ and a reference value of $N_{100\mu\text{mmax}}$ equal to 1, the index takes the value 1 when the ratio is equal to 0.1.

- Cost of the material

- 1) Cost of material produced in extruded round bars.
- 2) Payment Terms.
- 3) Change in the cost depending on the amount of material required.

- Availability of the material

- 1) Time required for the production and shipment of extruded bars of the selected material (as the order is received).

“ANALYTIC HIERARCHY PROCESS” AND CHOICE OF THE MATERIAL

The Analytic Hierarchy Process [3-13] was applied to the material selection, by assuming that it is produced in Italy by four companies, denominated for the sake of simplicity as A, B, C, D, with mechanical characteristics, costs and availability defined as follows. Table 1 shows the mechanical properties for the four companies.

Table 2 reports the values of the normalized quality indexes related to the mechanical characteristics, for the four considered companies.

Table 3 shows the material cost data for the four considered fictitious companies.

Table 4 reports the values of the data related to the material availability for the four considered companies.

CRITERIA FOR THE APPLICATION OF THE “ANALYTIC HIERARCHY PROCESS (AHP)” TO THE MATERIAL SELECTION

The first step is to define the aim of the search, or goal, while evaluating the different alternatives. In particular, for the choice of the composite material, the main goal is to identify the most suitable material based to specific needs. The alternatives are between the material manufacturers in Italy, *i.e.* the four companies denominated as A, B, C, D. Once the goal, under which the different alternatives must be evaluated, as well as the alternatives themselves, are defined, it is necessary to identify the basic parameters, *i.e.* the selection criteria for the choice of the material. The parameters are reported below, in one or more hierarchical categories, arranged at different levels, depending on their importance and their belonging to different decision criteria. In practice, by means of a schematic tree, the attributes are listed in the order they belong to a superior parameter. Therefore, in the problem of the choice of a material that uses a single category hierarchy, the main criterion for selection is the end of the research, *i.e.* the material choice. The second level presents the mechanical properties, the cost and the availability of same materials, while the third level lists the parameters strictly dependent from the second level attributes. For example, regarding the mechanical characteristics second level attribute, the third level presents the parameters $\frac{E}{\rho}$, $A\%$, $\frac{R_s}{\rho}$, $\frac{R_m}{\rho}$,

$$\frac{\sigma_{FA}}{\rho}, \frac{N_{100\mu\text{m}}}{n}, \frac{N_{100\mu\text{mmax}}}{n}.$$

Table 1. Mechanical characteristics for the four manufacturers of the composite material.

	A%	E [MPa]	R _m [MPa]	R _s [MPa]	σ _{FA}	N _{100 μm}	N _{100 μmmax}
A	4	92830	370	318	160	8	2
B	5	95000	350	300	140	12	1
C	7	88000	385	330	170	5	1
D	9	80000	360	305	150	9	2

Table 2. Values of the normalized quality indexes, related to the mechanical characteristics, for the four fictitious companies.

	A%	$\frac{E}{\rho}$	$\frac{R_m}{\rho}$	$\frac{R_s}{\rho}$	$\frac{\sigma_{FA}}{\rho}$	$\frac{N_{100\mu m}}{n}$	$\frac{N_{100\mu mmax}}{n}$
A	4	0.92	0.92	0.9	0.8	8	2
B	5	0.95	0.87	0.85	0.7	12	1
C	7	0.88	0.96	0.94	0.85	5	1
D	9	0.79	0.9	0.87	0.75	9	2

Table 3. Data related to the material costs for the four considered companies.

	Material Cost in Extruded Round Bars [€/kg]	Terms of Payment [Days]	Change in Cost with the Amount of Material [% Reduction for Every 1000 kg]
A	180	60	10
B	150	30	12
C	165	30	11
D	150	60	10

Table 4. Data on the availability of material for the four considered companies.

	Delivery Time [Days]
A	15
B	20
C	15
D	30

Subsequently, for each defined level in the hierarchy, priorities are assigned to different parameters level by level,

according to the importance assumed by the same parameters with respect to the decision criterion of the next higher level. For example, in the cost category it must be determined which one of the three cost parameters, *i.e.* 1) the cost of the material extruded bars, 2) the payment terms, and 3) changes in the cost with the amount of material, assumes a greater importance with respect to the other two, and it is necessary to establish the order of importance of three parameters.

To judge the importance of different parameters residing at the same hierarchical level, a grading scale is adopted, where the various possibilities of mutual significance, which different parameters may have between themselves, are classified in numeric terms (scale of 1 to 9). Table 5 shows

Table 5. Comparison of the numerical terms for parameters evaluation and literal meaning.

Importance	Definition	Explanation
1	Equal importance	The two parameters have the same importance within the same hierarchical level
3	Moderate importance	A parameter is considered to be moderately more important than the other
5	High importance	A parameter is considered to be more important than the other
7	Very high importance	A parameter is believed to be much more important than the other
9	Extreme importance	A parameter has extreme importance related to each other
2, 4, 6, 8	Intermediate importance between the previous values	Judgment of importance is intermediate between those reported

The result is justified by the fact that the assessment of priorities was the criterion used for judging the AHP methodology, and a higher priority was assumed for the mechanical properties, if compared to the cost of the

material, as well as the cost of the material with respect to availability.

The result turns out to be highly subjective, and tied to the importance of the value that the user assigns to the

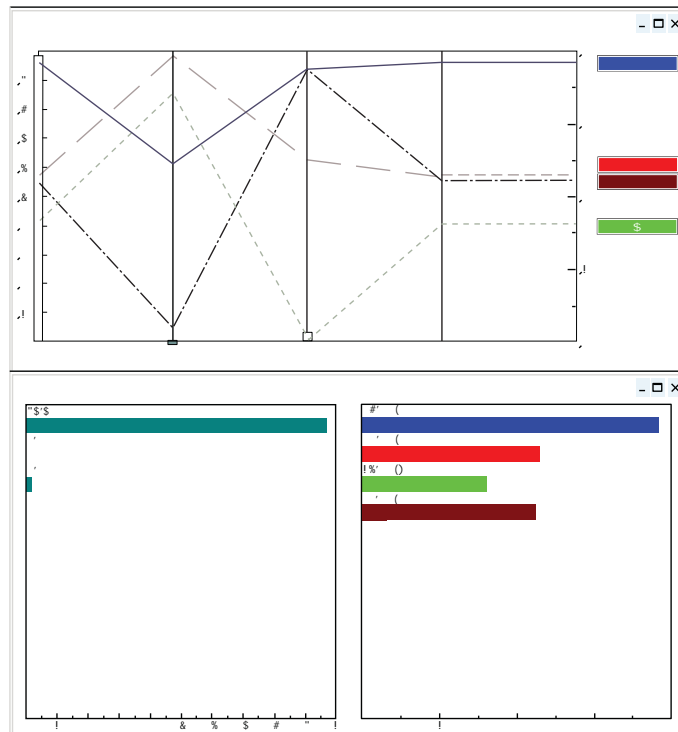


Fig. (8). Sensitivity analysis related to a high weight of the mechanical characteristics.

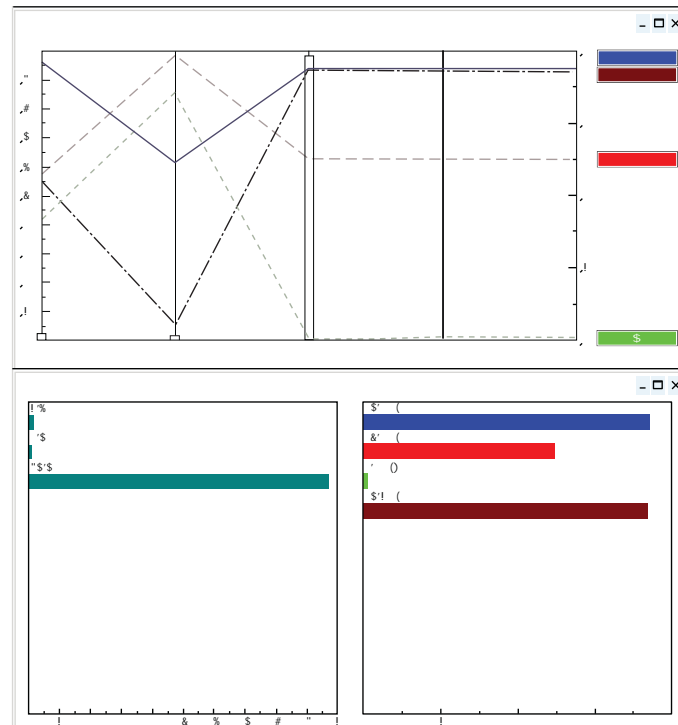


Fig. (9). Sensitivity analysis related to a high weight of the availability of the material.

different parameters that influence the choice of the material, thus being related to the user experience itself.

A sensitivity analysis of the various parameters can be carried out. By changing the priority of the individual parameters it is possible to evaluate their influence on the final choice. In Fig. (7), the material cost assumes a greater importance, if compared to the other parameters, and in this case the B company is the most competitive.

In Fig. (8), the mechanical characteristics assume a greater importance, if compared to the other parameters, and in this case the C company is the most competitive.

In Fig. (9), the availability of the material assumes a greater importance, if compared to the other parameters. In this case, the companies A and C appear to be the most competitive.

CONCLUSION

The multi-attribute decision AHP (Analytic Hierarchy Process) procedure was used for the choice of the best levels for the different parametric and non-parametric attributes and to select the best company. Parametric and non-parametric attributes were considered, and the AHP method allowed to choose the most attractive company and to develop the sensitivity analysis with respect to each parameter.

CONFLICT OF INTEREST

The author confirms that this article content has no conflict of interest.

ACKNOWLEDGEMENTS

Declared none.

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Received: June 5, 2014

Revised: July 16, 2014

Accepted: July 24, 2014

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